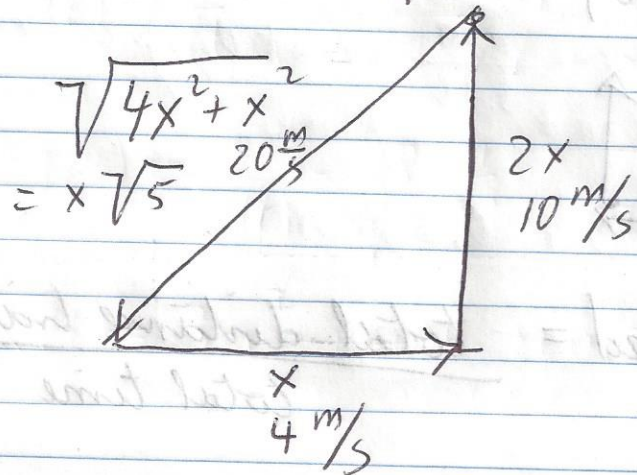


$$\bar{v}_{\text{speed}} = \frac{2x}{\frac{x}{4} + \frac{x}{2}}$$

$$v = \frac{x}{t}$$

$$t = \frac{x}{v}$$

$$= \frac{2}{\frac{1}{4} + \frac{1}{2}} = \frac{2}{\frac{3}{4}} = \frac{8}{3} \frac{\text{m}}{\text{s}}$$



$$= 2.667 \frac{\text{m}}{\text{s}}$$

$$\bar{v}_{\text{speed}} = \frac{x + 2x + x\sqrt{5}}{\frac{x}{4} + \frac{2x}{10} + \frac{x\sqrt{5}}{20}} =$$

$x(t)$

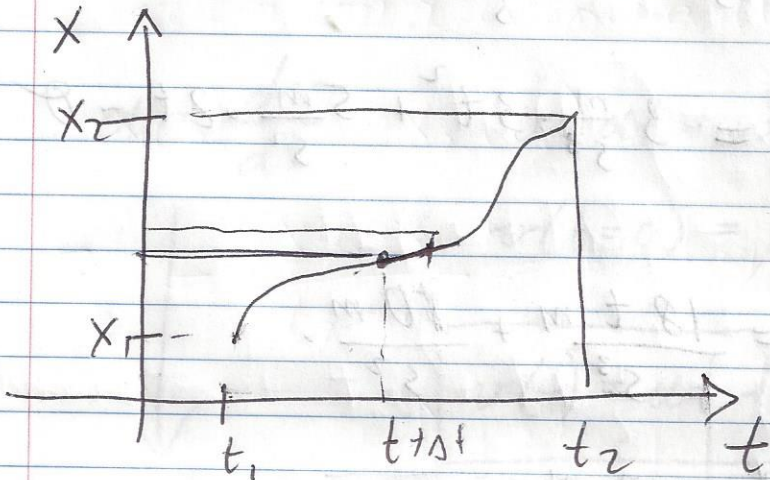
$$\bar{v} = \frac{x_2 - x_1}{t_2 - t_1} = \frac{x_1(t_1 + \Delta t) - x_1(t_1)}{\Delta t}$$

$\Delta t = t_2 - t_1$ change in t

$$\frac{1 \text{ m}}{2} = \frac{1 \text{ m}}{2 \text{ s}} = \bar{v}$$

Make $\Delta t \rightarrow 0$

$$v(t) = \lim_{\Delta t \rightarrow 0} \frac{x(t+\Delta t) - x(t)}{\Delta t} = \frac{dx}{dt}$$



$$\bar{a} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{v_1(t_1 + \Delta t) - v_1(t_1)}{\Delta t}$$

↑
number

$$a(t) = \lim_{\Delta t \rightarrow 0} \frac{v_1(t_1 + \Delta t) - v_1(t_1)}{\Delta t} = \frac{dv}{dt}$$

$$a(t) = \frac{dv}{dt}$$

$$j(t) = \frac{da}{dt} \quad \text{jerk}$$

$$x(t) = 3t^3 + 5t^2 - 5$$

$$x(t) = 3 \frac{m}{s^3} t^3 + \frac{5m}{s^2} t^2 - 5m$$

$$v(t) = \frac{dx}{dt} = 3 \frac{m}{s^3} \cdot 3t^2 + \frac{5m}{s^2} \cdot 2t - 0$$

$$a(t) = \frac{dv}{dt} = \frac{18t m}{s^3} + \frac{10m}{s^2}$$

$$j(t) = \frac{da}{dt} = 18 \frac{m}{s^3}$$

$$x(t) = 3m \sin \omega t \quad \sin\left(\frac{5}{s}t\right) \quad \frac{5}{s} = \omega$$

$\omega =$
angular
frequency

$$v(t) = \frac{dx}{dt} = 3m \cos\left(\frac{5}{s}t\right) \cdot \frac{5}{s}$$

$$= 15 \frac{m}{s} \cos\left(\frac{5}{s}t\right)$$

$$a(t) = \frac{dv}{dt} = 15 \frac{m}{s} \left(-\sin\frac{5}{s}t\right) \cdot \frac{5}{s}$$

$$= -75 \frac{m}{s^2} \sin\frac{5}{s}t$$

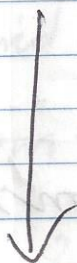
Kinematics: acceleration $a = \text{constant}$.

Can we determine $v(t)$ and $x(t)$ by using just the definitions?

$$a = \frac{dv}{dt}$$

$$v = at + \text{constant} = v(t)$$

$$v(t=0) = \text{constant} = v_0$$



$$v(t) = at + v_0$$

$$dv = a \cdot dt$$

$$\int dv = \int a \cdot dt$$

$$\int dx$$



integration symbol.

$$v(t) = at + v_0$$

$$\int_{v_0}^{v_1} dv = \int_{t_0}^{t_1} a dt$$

$$v_1 - v_0 = at_1 - at_0$$

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kinematics = motion problems: constant

$$v(t) = at + v_0$$

$$v(t) = \frac{dx}{dt}$$

$$\int dx = \int v(t) \cdot dt$$

$$= \int (at + v_0) dt$$

$$x(t) = \frac{1}{2} at^2 + v_0 t + \text{constant}$$

$$x(t) = \frac{1}{2} at^2 + v_0 t + x_0$$

Example: You ride a bike at 20 mph

You accelerate for 5 s with $a = 5 \frac{m}{s^2}$

You start at $x(t=0) = 0$

where are you after 5 seconds?

What is your speed or velocity?

$$\frac{20 \text{ miles}}{\text{hour}} = 20 \cdot \frac{1610 \text{ m}}{3600 \text{ s}} = 20 \cdot 0.447 = 8.94 \frac{m}{s}$$

$$x(5s) = \frac{1}{2} \cdot 5 \frac{m}{s^2} \cdot 25s^2 + 8.94 \frac{m}{s} \cdot 5s + 0 = 107 \text{ m}$$

$$v = at + v_0$$

$$= 5 \frac{\text{m}}{\text{s}^2} \cdot 5 \text{s} + 8.94 \frac{\text{m}}{\text{s}}$$

$$= 33.94 \frac{\text{m}}{\text{s}}$$

At what speed are you going at $x = 60 \text{ m}$?

Find the time first:

$$60 \text{ m} = \frac{1}{2} \cdot 5 \cdot t^2 + 8.94 t$$

$$2.5t^2 + 8.94t - 60 = 0$$

$$t = \frac{-8.94 \pm \sqrt{8.94^2 + 4 \cdot 2.5 \cdot 60}}{5}$$

$$= \frac{-8.94 \pm \sqrt{680}}{5}$$

$$= \frac{-8.94 \pm 26.1}{5} = -1.79 \pm 5.22$$

$$= \underline{\underline{3.43 \text{ s}}}$$

$$v = at + v_0$$

$$= 5 \frac{\text{m}}{\text{s}^2} \cdot 3.44 \text{ s} + 8.94 = \underline{\underline{26.1 \frac{\text{m}}{\text{s}}}}$$

Eliminate t from our equations

$$\begin{cases} x = \frac{1}{2}at^2 + v_0t + x_0 \\ v = at + v_0 \end{cases}$$

$$t = \frac{v - v_0}{a}$$

$$x - x_0 = \frac{1}{2}a \left(\frac{v - v_0}{a} \right)^2 + v_0 \left(\frac{v - v_0}{a} \right) \quad | \cdot 2a$$

$$2a(x - x_0) = (v - v_0)^2 + 2v_0(v - v_0)$$

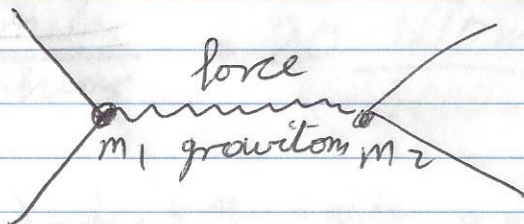
$$(x - x_0) \cdot 2a = v^2 - 2v_0v + v_0^2 + 2v_0v - 2v_0^2$$

$$= v^2 - v_0^2$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

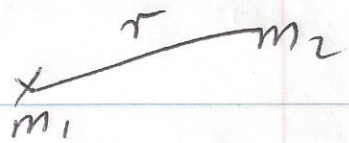
Newton's law of gravitation:
= gravitational attraction between any
two objects with a mass or energy.

$$E = mc^2$$



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$$F = \frac{G m_1 m_2}{r^2}$$



m_1 is a man on the surface of the earth
 m_2 is the mass of the earth

$$F = m_1 \left(\frac{G m_2}{r^2} \right) = m_1 \frac{.6673 \cdot 10^{-11} \cdot 5.99 \cdot 10^{24}}{(6.37 \cdot 10^6)^2}$$
$$g = m_1 \cdot 9.85 \frac{m}{s^2}$$

$$\boxed{g = 9.86 \frac{m}{s^2}}$$